

Compositions in $\mathbf{Mnd}(\mathcal{K})$

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- The identity 1-cell on a 0-cell (\mathcal{A}, T) is given by: $(\text{Id}_{\mathcal{A}}, \text{id}_T) : (\mathcal{A}, T) \rightarrow (\mathcal{A}, T)$.
- The identity 2-cell on a 1-cell $(X, \psi_{T,X}) : (\mathcal{A}, T) \rightarrow (\mathcal{A}', T')$ is given by id_X .